

30 1. Block 1: Topography/bathymetry (hv = no vertical spacing; hh = 1 km) 2. Block 2: -4 km to 30 km depth (hv = 200 m; hh= 1 km). The depth range of this block is large enough to contain the highest point in topography and the lowest point in bathymetry. 3. Block 3: 30 to 70 km (hv = 300 m; hh= 1 km) 4. Block 4: 70 to 100 km (hv = 400 m; hh= 1km) 5. Block 5: 100 to 200 km (hv = 500 m; hh= 1 km) S3. Choosing the Grid spacing (h) The choice of grid spacing is very important in SW4 as it determines the maximum frequency the model can resolve. It is related to the minimum shear wave velocity in the 41 domain by h=minVs/(PPW×f_{max}); where minVs is the minimum shear wave velocity, PPW is the 42 Point Per Wavelength and f_{max} is the maximum frequency in the simulation. According to SW4 manual, the recommendation is that the PPW must be at least 8 for stable wave solutions. If we use a maximum frequency of 0.5 Hz while minimum Vs in the 3D velocity model is 350 m/s, h is 87.5m. Based on the size of the domain geometry, this grid spacing will make the computational cost very expensive. 47 We increase the minimum shear wave velocity to 1200 m/s based on the average Vs in the upper 400 km in the 3D structure to decrease the computational cost and memory usage. Using this minimum Vs gives h of 600 m and 300 m for 0.25 Hz and 0.50 Hz simulation, respectively. We use 'refinement' command in SW4 to increase the grid spacing with depth to reduce computational cost since the velocity increases with depth and the velocity model becomes more homogeneous with depth. To maintain similar PPW for each block in the block boundary, we plot a profile of the Vs at different points in the 3D structure to determine optimal location of the block boundaries, usually where the minVs doubles (Fig. S5). The figure shows that the minVs increases to about 2800 m/s below 25 km and stays constant with depth to 200 km depth. This is due to the lower velocity value of the subducting slab compares with the surrounding higher velocity rocks with depth. We setup refinement level at 75 depth. For the 0.50 Hz simulations, for example, we use

- a curvilinear mesh of 300 m grid size in the upper 30 km depth, and Cartesian mesh below 30
- 60 km with a grid spacing of 300 m in the upper $30 75$ km depth and 600 m from 75-200 km
- depth.

Fig. S1: Fault mesh of the Slab 2.0 model of Kuril region of the Japan Trench using GMSH. Each

triangle shows the subfaults and the different colors show the partition of the Japan Trench for

- determining regular and undistorted mesh, but do not have any geological inference.
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 Fig. S2: Mapping of the planar Ibaraki 2011 SRCMOD rupture (Kubo et al., 2013) on the non- planar Japan trench geometry from Slab 2.0 model. Blue dots represent the location of the center of each subfault outlining the Japan Trench while the square pattern regions in the two subplots show the dip and strike slips of the Ibaraki 2011 SRCMOD rupture model, respectively.

Ibaraki 2011 (Zheng Rupture Model)

Iwate 2011 (Zheng Rupture Model)

Fig. S4: Same as Figure S3, but for Iwate 2011 (Zheng model), Tokachi 2003 (Hayes and

SRCMOD models).

Fig. S5: SW4 domain for the 0.50 Hz simulations showing the (A-D) selected GNSS stations

(colored by the observed signal-to-noise ratio) and surface-projection of the FakeQuake

ruptures for each earthquake, and the observed Signal-to-Noise ratio (SNR) with distance.

Figure S5E shows the domain geometry showing the grid spacing, the refinement layer and

89 types of mesh used in the simulations. We used a curvilinear mesh for the topography/

bathymetry to a depth of 30 km, and cartesian mesh below 30 km with 300 m grid spacing from

30-75 km depth, and 600 m from 75 – 200 km depth.

Figure S6: Effect of the choice of 1D velocity model used for the 1D simulations on PGD

- residuals using three 1D velocity models used by two other researchers: Zheng et al. (2020) and
- Koketsu et al. (2004). On each boxplot, residuals for each model are shown as patterned box
- 97 and whisker plots. The blue, orange and light blue boxplots represent the PGD residuals for
- Hayes (20017), Koketsu et al. (2014) and Zheng et al. (2020) studies, respectively. The red
- horizontal line represents the zero residual line.

 Fig. S7: (left) Profiles of the material properties at location x=10 km and y= 10 km in the 3D Japan Integrated Velocity Structure Model (Koketsu et al., 2008, 2009), while (right) shows all 104 the Vs profiles at different locations within the 3D structure showing the variation of minimum 105 shear wave velocity with depth.

 $\begin{array}{c} 107 \\ 108 \end{array}$ 108 Fig. S8: The PGD, t_{PGD} , SD residuals and cross correlation map showing the spatial variation of the 3D residuals for the Ibaraki 2011 earthquake for Rupture 5 of the 100 FakeQuake ruptures

the 3D residuals for the Ibaraki 2011 earthquake for Rupture 5 of the 100 FakeQuake ruptures

110 using the SRCMOD mean rupture model (Kubo et al., 2013).

 Fig. S9: Comparing MudPy 1D vs SW4 3D residuals between the synthetic to observed GNSS waveforms for Ibaraki 2011 (Zheng), Miyagi 2011 (Zheng) and Tokachi 2003 (SRCMOD3). Figure 114 (A-C) PGD residuals, (D-F) t_{PGD} (s) residuals, (G-I) static displacement residuals and (J-L) cross correlation values. We compare only the residuals of two corresponding rupture models in the MudPy and SW4 synthetic simulations. The blue boxplots with circle hatched style represents the MudPy 1D residuals while the orange boxplot (diamond hatch style) represents the SW4 3D simulation. The red horizontal line represents the zero residual line.

- 119 Table S1: P- and S-wave velocities (Vp and Vs), density (ρ) and P- and S-wave quality factors (Qp
- 120 and Qs) for the 23 layers in the 3D Japan Integrated Velocity Structure Model (Koketsu et al.,
- 121 2008, 2009).

